

MOOC@TU9

## Week 9 - The Rise of Small Satellites

How much power do our solar panels need to generate?

$T$  = orbit period

$T_d$  = time in sunlight (day)

$T_e$  = eclipse time (night)

$P_e, P_d$  = power consumption (eclipse/ day)

$P_{SA}$  = power generation by solar array

$\eta_e/\eta_d$  = efficiency of the power subsystem (eclipse / day)

$\eta_e = 0.65$

$\eta_d = 0.85$

$R$  = earth radius = 6378km

$h$  = orbit height = 500km

$GM = 398\,600 \frac{km^3}{s^2}$

$$\begin{aligned} T &= 2\pi \sqrt{\frac{(R+h)^3}{GM}} = 2\pi \sqrt{\frac{(6378km+500km)^3}{398\,600 \frac{km^3}{s^2}}} = 2\pi \sqrt{816,298.92 s^2} \\ &= 2\pi \cdot 903.5 s = 5677 s \end{aligned}$$

$$T_e = \frac{T}{\pi} \arcsin\left(\frac{R}{R+h}\right) = \frac{5677 s}{\pi} \arcsin\left(\frac{6378}{6878}\right) = 2145 s$$

$$T_d = T - T_e = 5677s - 2145s = 3532s$$

$$\begin{aligned} P_{SA} &= \frac{1}{T_d} \left( \frac{P_e T_e}{\eta_e} + \frac{P_d T_d}{\eta_d} \right) = \frac{1}{3532s} \left( \frac{P_e \cdot 2145s}{0.65} + \frac{P_d \cdot 3532s}{0.85} \right) \\ &= \frac{P_e \cdot 3300 + P_d \cdot 4155}{3532} = 0.934 \cdot P_e + 1.176 \cdot P_d \end{aligned}$$